

**Geometry/Trigonometry:**

$$\cos(30^\circ) = \frac{1}{2}\sqrt{3} \quad \sin(30^\circ) = \frac{1}{2} \quad \tan(30^\circ) = \frac{1}{3}\sqrt{3}$$

$$\cos(45^\circ) = \frac{1}{2}\sqrt{2} \quad \sin(45^\circ) = \frac{1}{2}\sqrt{2} \quad \tan(45^\circ) = 1$$

$$\cos(60^\circ) = \frac{1}{2} \quad \sin(60^\circ) = \frac{1}{2}\sqrt{3} \quad \tan(60^\circ) = \sqrt{3}$$

$$\cos\left(\frac{1}{2}\pi - \theta\right) = \sin(\theta) \quad \sin\left(\frac{1}{2}\pi - \theta\right) = \cos(\theta)$$

$$\cos(2\theta) = 1 - 2\sin^2(\theta) \quad \sin(2\theta) = 2\sin(\theta)\cos(\theta)$$

	circle	sphere
circumference	$2\pi r$	
(surface) area	$\pi r^2$	$4\pi r^2$
volume		$\frac{4}{3}\pi r^3$

**Integrating and Differentiating:**

$$\frac{d(x^n)}{dx} = nx^{n-1}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1}$$

**Linear Motion in One Dimension (general):**

$$v = \frac{dx}{dt}$$

$$a = \frac{dv}{dt} = \frac{d^2x}{dt^2}$$

**Linear Motion in One Dimension (special case):**

$$a(t) = a = \text{constant}$$

$$v(t) = v_0 + at$$

$$x(t) = x_0 + v_0t + \frac{1}{2}at^2$$

**Linear Motion in Two/Three Dimensions:**

$$\vec{v} = \frac{d\vec{r}}{dt}$$

$$\vec{a} = \frac{d\vec{v}}{dt} = \frac{d^2\vec{r}}{dt^2}$$

**Circular Motion:**

$$a_R = \frac{v^2}{r}$$

$$a_{\text{tan}} = \frac{dv}{dt}$$

**Force Laws:**

$$\sum_i \vec{F}_i = m\vec{a} \quad \text{Newton's Second Law of Motion}$$

$$\vec{F}_{12} = -\vec{F}_{21} \quad \text{Newton's Third Law of Motion}$$

**Friction:**

$$F_s \leq \mu_s N \quad \text{Static Friction}$$

$$F_k = \mu_k N \quad \text{Kinetic Friction}$$

$$F_D = -bv \quad \text{Dragg Force}$$

**Newton's Gravitational Law:**

$$\vec{F}_{12} = -G \frac{m_1 m_2}{r_{21}^2} \hat{r}_{21}$$

**Kepler's Third Law (Law of Periods):**

$$\left(\frac{T_1}{T_2}\right)^2 = \left(\frac{r_1}{r_2}\right)^3$$

**Work Done by a Force:**

$$W = \vec{F} \cdot \vec{d} \quad \text{Constant Force}$$

$$W = \int_a^b \vec{F} \cdot d\vec{l} \quad \text{Variable Force}$$

**Translation Kinetic Energy:**

$$K = \frac{1}{2} m v^2$$

**Work-Energy Theorem:**

$$W = \Delta K$$

**Potential Energy:**

$$\Delta U = U_2 - U_1 = -\int_1^2 \vec{F} \cdot d\vec{l} = -W \quad \text{General Definition of Potential Energy}$$

$$\vec{F} = -\frac{dU}{dx} \hat{x} - \frac{dU}{dy} \hat{y} - \frac{dU}{dz} \hat{z}$$

$$U(h) = mgh \quad \text{Gravitational Potential Energy (Close to the Surface)}$$

$$U(r) = -G \frac{mM_E}{r} \quad \text{Gravitational Potential Energy } (r > r_E)$$

$$U(x) = \frac{1}{2} kx^2 \quad \text{Spring with Spring Constant } k$$

**Conservation of Energy:**

$$\Delta U + \Delta K = 0 \quad \text{Conservation of Mechanical Energy}$$

$$\Delta U + \Delta K = W_{NC} \quad \text{Conservation of Energy}$$

**Power:**

$$P = \frac{dW}{dt}$$

**Linear Momentum and Newton's Second Law:**

$$\vec{p} = m\vec{v}$$

$$\frac{d\vec{p}}{dt} = \sum \vec{F}$$

**Collision Impulse:**

$$\vec{J} = \int_{t_1}^{t_2} \vec{F} dt = \vec{p}_f - \vec{p}_i = \Delta\vec{p}$$

**Elastic Collisions in One Dimension:**

$$v_1' = v_1 \left( \frac{m_1 - m_2}{m_1 + m_2} \right) + v_2 \left( \frac{2m_2}{m_1 + m_2} \right)$$

$$v_2' = v_1 \left( \frac{2m_1}{m_1 + m_2} \right) + v_2 \left( \frac{m_1 - m_2}{m_1 + m_2} \right)$$

**Center of Mass:**

$$\vec{r}_{cm} = \frac{\sum_i m_i \vec{r}_i}{\sum_i m_i}$$

$$\vec{r}_{cm} = \frac{1}{M} \int \vec{r} dm$$

**Motion of the Center of Mass:**

$$M\vec{a}_{cm} = \sum \vec{F}_i$$

**Rocket Equations:**

$$M \frac{d\vec{v}}{dt} = \sum \vec{F}_{ext} + \vec{v}_{rel} \frac{dM}{dt}$$

$$Ma_{rocket} = RU_0 \quad \text{First Rocket Equation}$$

$$v_f = v_i + u \ln \left( \frac{M_i}{M_f} \right) \quad \text{Second Rocket Equation}$$