

## Quantum Mechanics I - Module 7

1. Define the following operators:

$$L^2 = L_x^2 + L_y^2 + L_z^2 \quad L_{\pm} = L_x \pm iL_y$$

Work out the following commutators. Try to use as many shortcuts as possible!

- (a)  $[L_z, x]$
- (b)  $[L_z, y]$
- (c)  $[L_z, z]$
- (d)  $[L_z, p_x]$
- (e)  $[L_z, p_y]$
- (f)  $[L_z, p_z]$
- (g)  $[L_x, L_y]$
- (h)  $[L^2, L_x]$
- (i)  $[L_z, L_{\pm}]$
- (j)  $[L^2, L_{\pm}]$
- (k)  $[L_z, r^2]$
- (l)  $[L_z, p^2]$

2. Use the previous question to show that the Hamiltonian

$$H = \frac{p^2}{2m} + V(r)$$

commutes with all three components of  $L$  provided that  $V$  depends only on  $r$ .

3. Considering the hydrogen atom, what do you think the following equation means?

$$H|211\rangle = E_2|211\rangle$$

Write this equation as you are used to seeing it.