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# Classical Mechanics

## Phy 235, Lecture 08.

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# February 1 (my father's birthday): the flood of 1953.



In 1953, my father was in the army and was sent to rescue people and rebuild dikes.



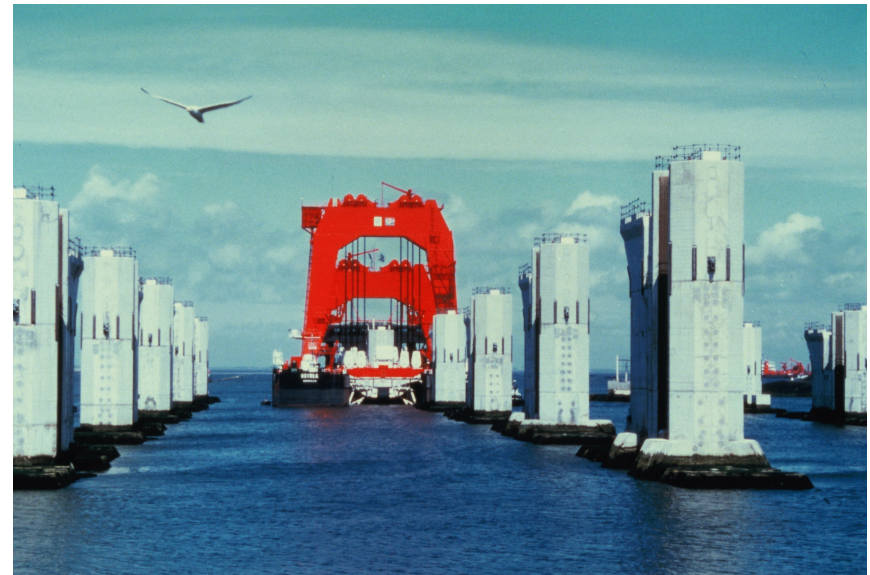
20 days after the flood: plans were developed.  
**De Delta Werken** were completed in 1997.



# An example: Oosterscheldekering, 9 km long.



After constructing the pillars, flood the construction area and pick up the pillars.



# Laying a carpet. Putting down pillars.

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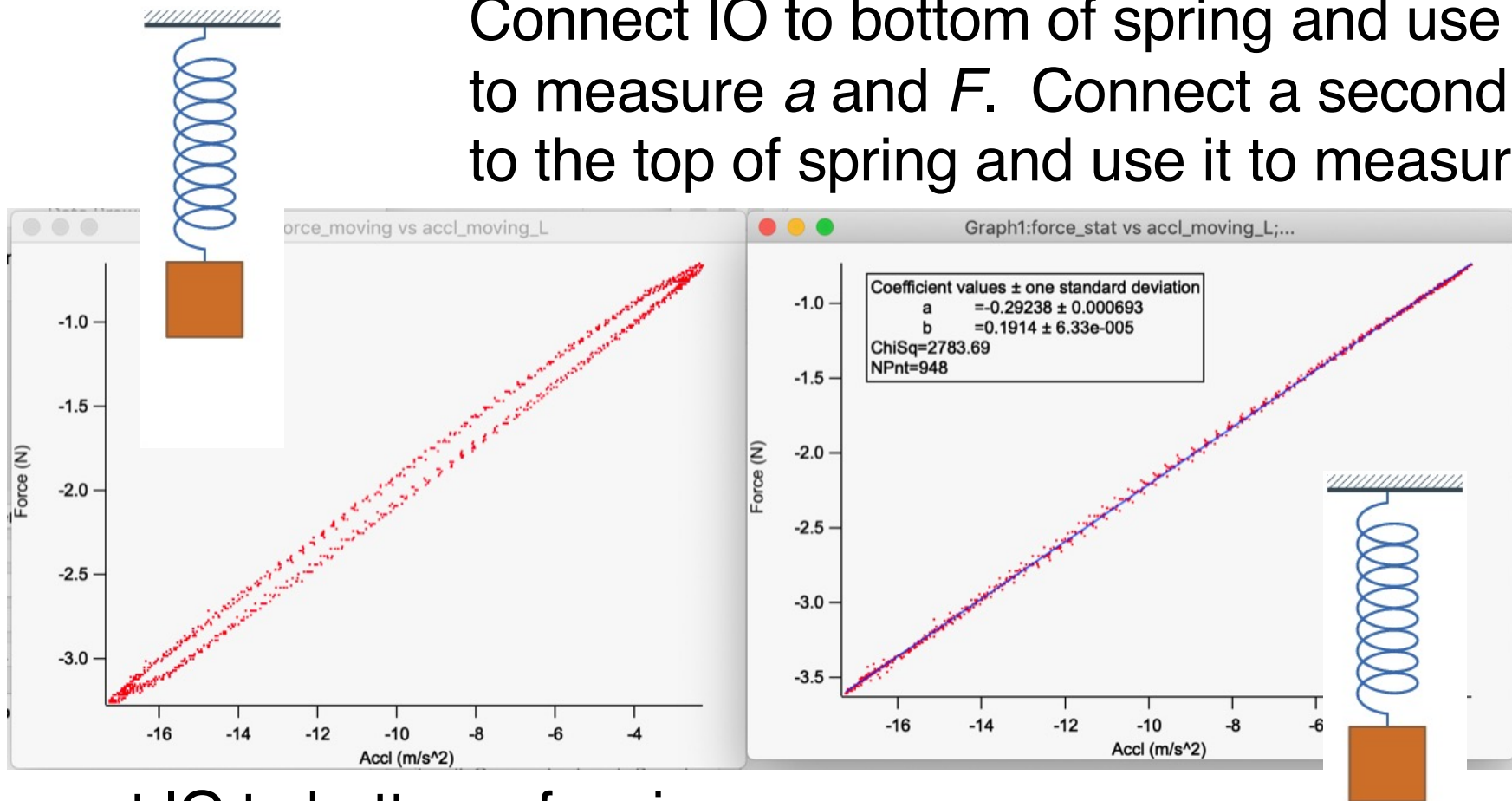
Done.





# Before Chapter 6 ..... Spring oscillations. Inertial frames and non-inertial frames.

Connect IO to bottom of spring and use it to measure  $a$  and  $F$ . Connect a second IO to the top of spring and use it to measure  $F$ .



Connect IO to bottom of spring  
and use it to measure  $a$  and  $F$ .

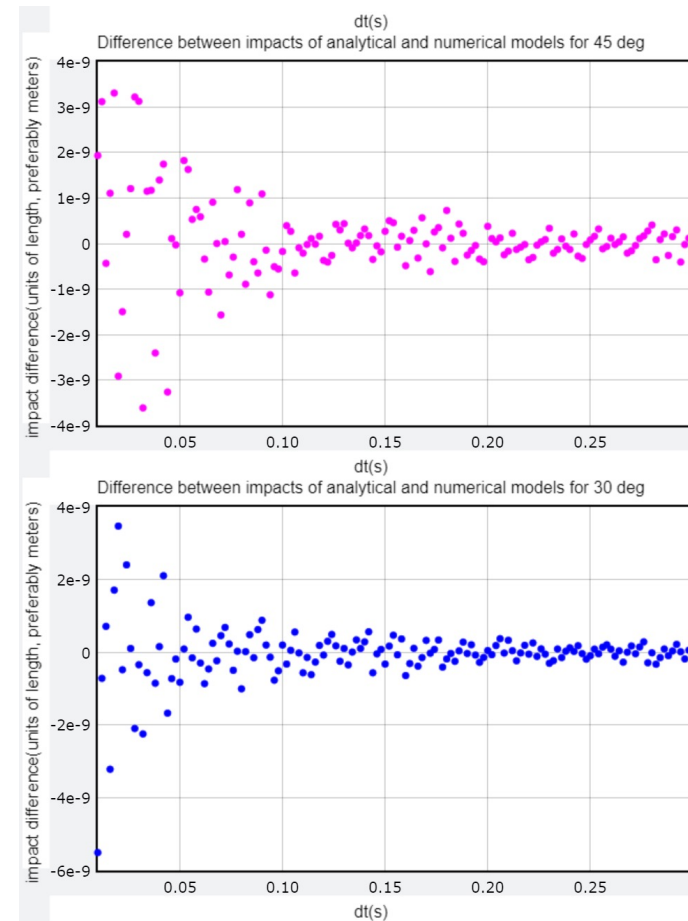
# Before Chapter 6 . . . . .

## Optional homework assignment.

- **Interesting observations:**
  - When you compare the range with the analytical solution, you see the impact of rounding errors.
  - It appears that the product of thrust force times time is constant.

Force constant F (kg/s)	Time of thrust T (t)
3.0	42.0
4.0	32.0
5.0	25.0
6.0	20.5
7.0	17.5
8.0	15.5
9.0	14.0
10.0	12.5
15.0	8.25
20.0	6.25
25.0	6.2
50.0	2.2

Table of combinations of F and T that produce an impact point in the numerical projectile approximately equal to that of the analytical projectile

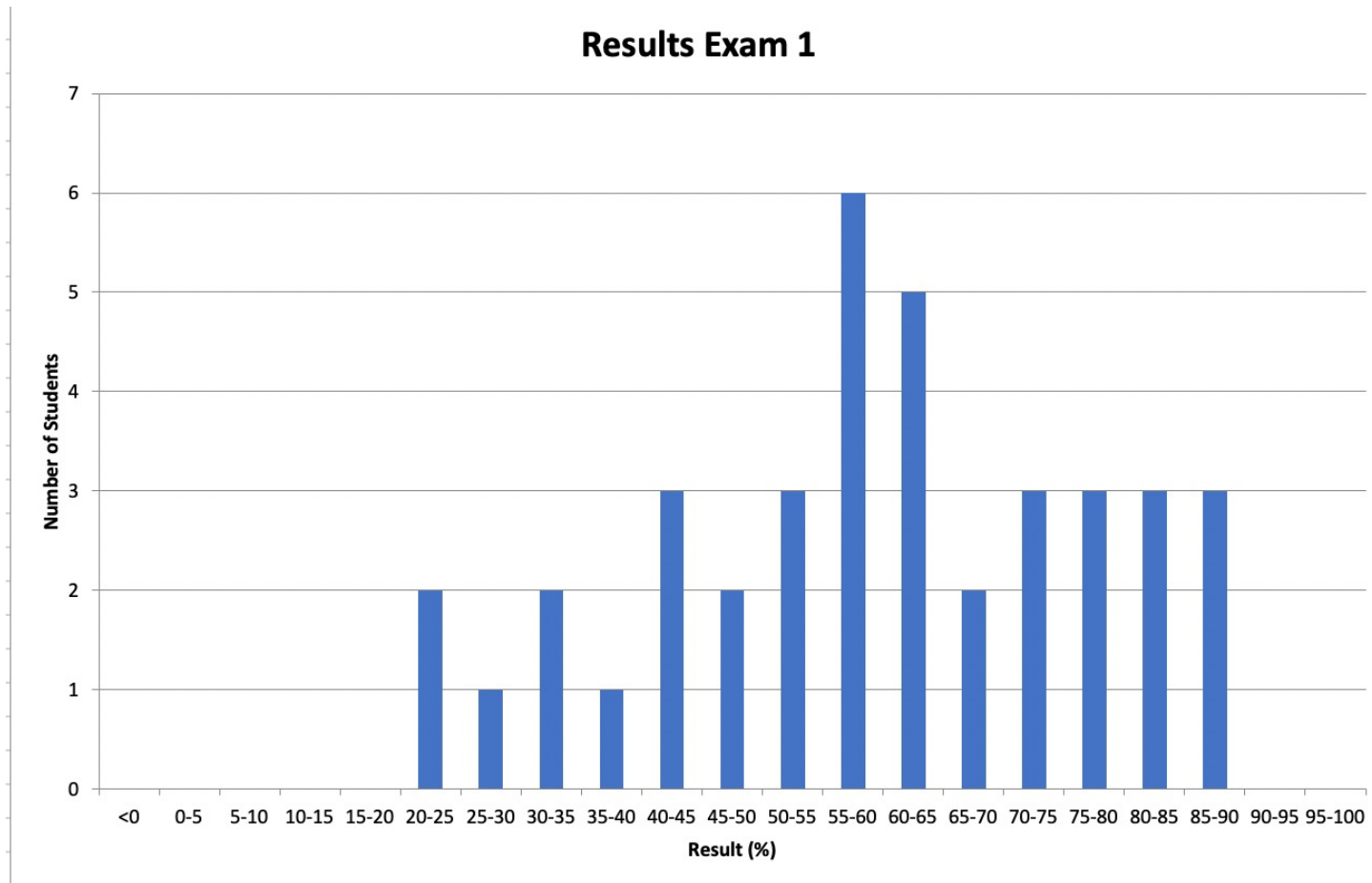


# Results Exam # 1

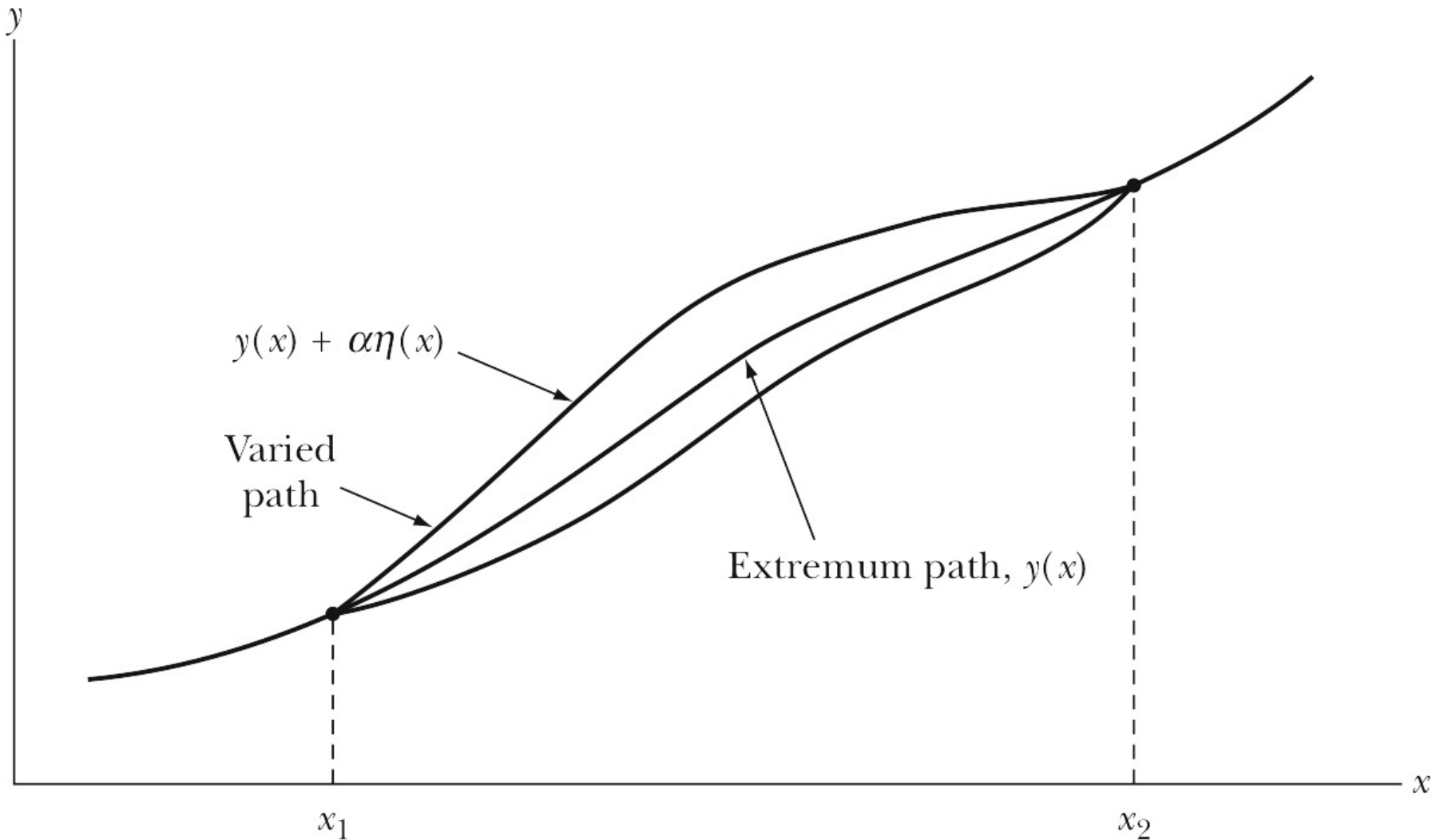
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- Question 1:
  - Average = 19 out of 25.
  - Example problem in book.
- Question 2:
  - Average = 14 out of 25.
  - End-of-chapter problem.
- Question 3:
  - Average = 10 out of 25.
  - Discussed during class.
- Question 4:
  - Average = 16 out of 25.
  - NAP = Nieuw Amsterdams Peil!

# Exam 1

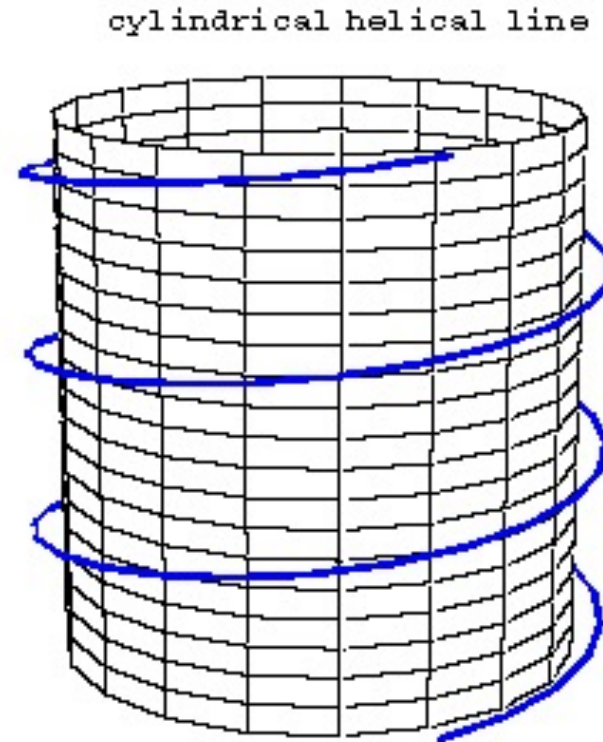


# Calculus of Variations.



## Problem 6.4

- Show that the geodesic on the surface of a right circular cylinder is a segment of a helix.



[https://www.encyclopediaofmath.org/index.php/Helical\\_line](https://www.encyclopediaofmath.org/index.php/Helical_line)



## 2 Minute 19 Second Intermission.

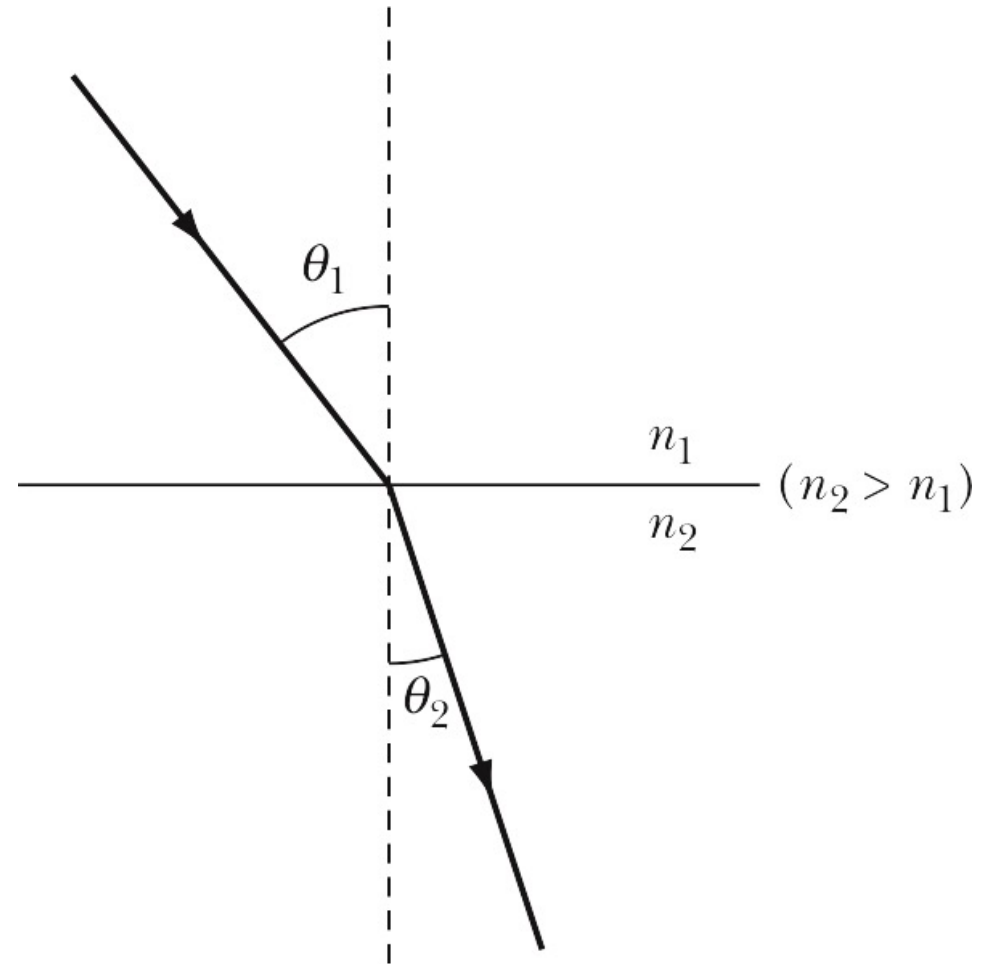
- Since paying attention for 1 hour and 15 minutes is hard when the topic is physics, let's take a 2 minute 19 second intermission.
- You can:
  - Stretch out.
  - Talk to your neighbors.
  - Ask me a quick question.
  - Enjoy the fantastic music.



## Problem 6.7

- Consider light passing from one medium with index of refraction  $n_1$  into another medium with index of refraction  $n_2$ .
- Use Fermat's principle to minimize time, and derive the law of refraction:

$$n_1 \sin \theta_1 = n_2 \sin \theta_2.$$





## Second Euler's Equation.

- The first version of Euler's equation is:

$$\frac{\partial f}{\partial y} - \frac{d}{dx} \left( \frac{\partial f}{\partial y'} \right) = 0$$

- The second version of Euler's equation is useful when  $f$  does not explicitly depend on  $x$ .
- The second version of Euler's equation is:

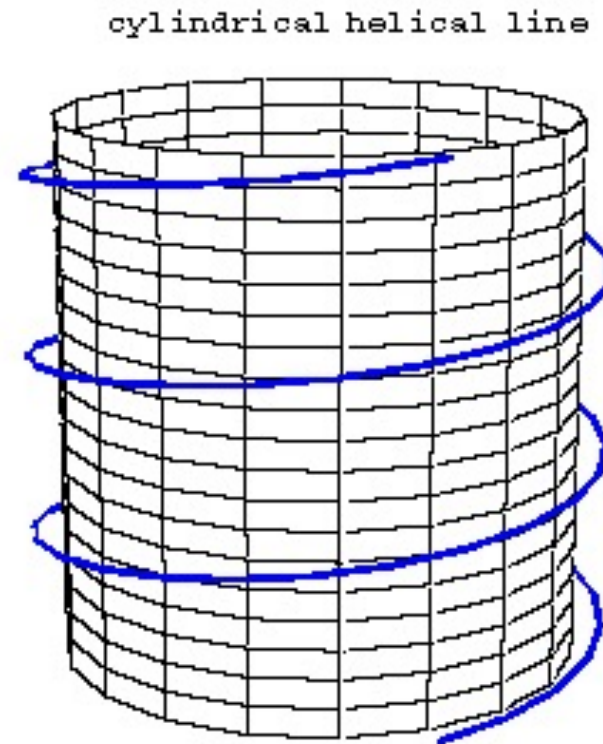
$$\frac{\partial f}{\partial x} - \frac{d}{dx} \left( f - y' \frac{\partial f}{\partial y'} \right) = 0$$

- When  $f$  does not explicitly depend on  $x$  this equation becomes:

$$f - y' \frac{\partial f}{\partial y'} = \text{constant}$$

## Problem 6.4

- Show that the geodesic on the surface of a right circular cylinder is a segment of a helix.
- Now use Euler's second equation.



[https://www.encyclopediaofmath.org/index.php/Helical\\_line](https://www.encyclopediaofmath.org/index.php/Helical_line)

# More than one dependent variable.

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- Consider the function  $f$  which depends on several dependent variables  $y_1, y_2, y_3$ , etc.
- In this case, to minimize the path integral of  $f$ , the dependent variables must satisfy the following condition:

$$\frac{\partial f}{\partial y_i} - \frac{d}{dx} \left( \frac{\partial f}{\partial y_i'} \right) = 0$$

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# ENOUGH FOR TODAY?