

---

# Classical Mechanics

## Phy 235, Lecture 03.

Frank L. H. Wolfs  
Department of Physics and Astronomy  
University of Rochester

A great image,  
to start a great lecture.



# Course Information.

---

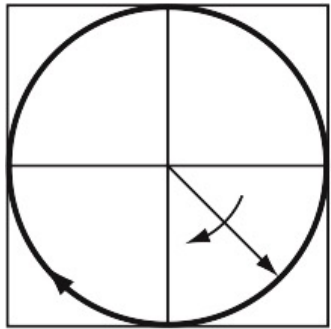
- All homework solutions will be available on the Phy 235 website. They are password protected (see email for details).
  - <http://teacher.pas.rochester.edu/PHY235/HomeWork/Solutions/>
- The graphs required for homework set # 2 can be made using various programs (including Excel). The installation package or Igor is available on the Phy 235 website:
  - <http://teacher.pas.rochester.edu/PHY235/DownloadFolder/Software/SoftwareIndex.htm>
- The VPython code used during lectures can be found at the following URL:
  - <http://teacher.pas.rochester.edu/PHY235/ComputingTools/ComputingToolsIndex.htm>

# Chapter 3

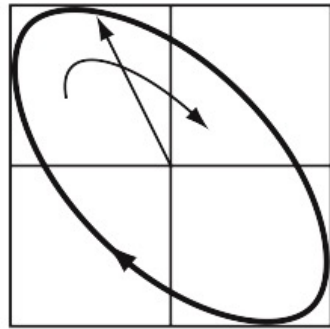
---

- Harmonic motion:
  - Motion around a position of stable equilibrium.
  - Simple harmonic motion (the focus today):
    - At small distances around the equilibrium position, the force is approximately equal to  $-kx$ .
    - The total energy of the system is constant. The kinetic and potential energy will be time dependent.
  - Damped and driven harmonic motion (the focus of Wednesday next week):
    - Damped harmonic motion occurs when friction or drag forces are acting on the system. Energy is dissipated and the system will gradually come to rest.
    - Driven harmonic motion adds a driving force in order to compensate for damping losses.

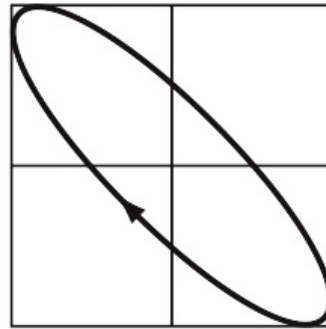
# Two-dimensional Simple Harmonic Motion. $y$ vs $x$ for single restoring force.



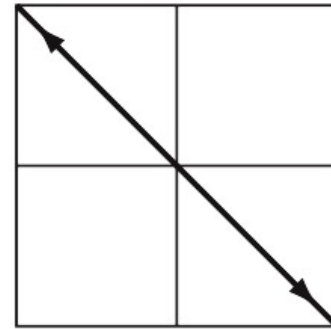
$\delta = 90^\circ$



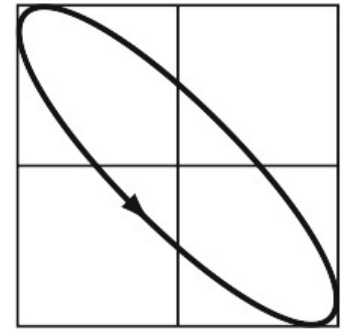
$\delta = 120^\circ$



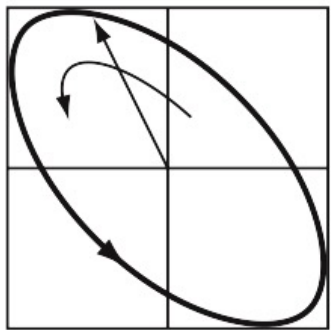
$\delta = 150^\circ$



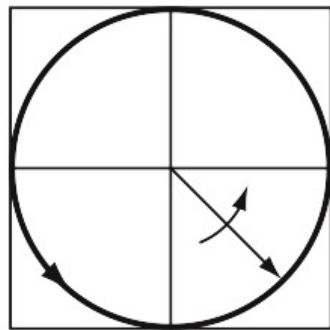
$\delta = 180^\circ$



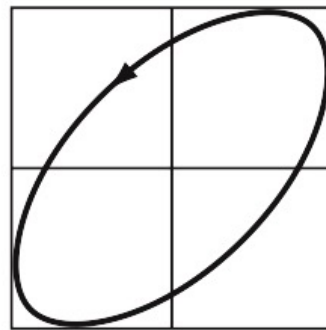
$\delta = 210^\circ$



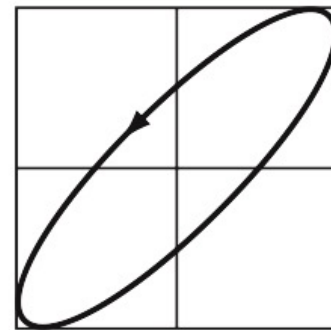
$\delta = 240^\circ$



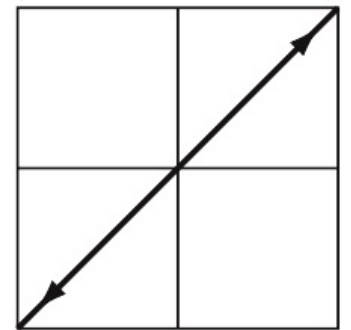
$\delta = 270^\circ$



$\delta = 300^\circ$

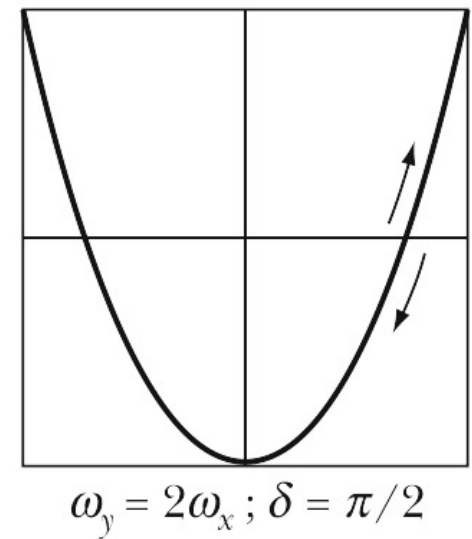
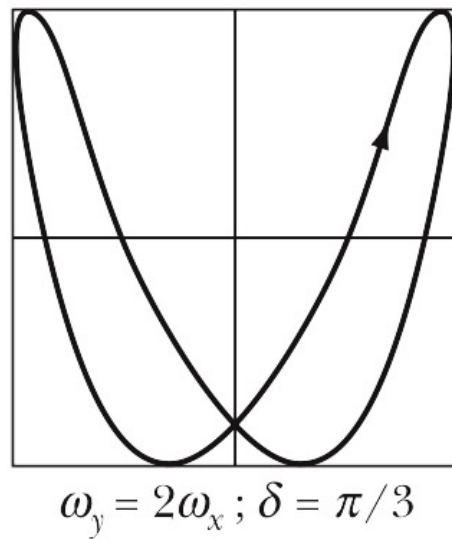
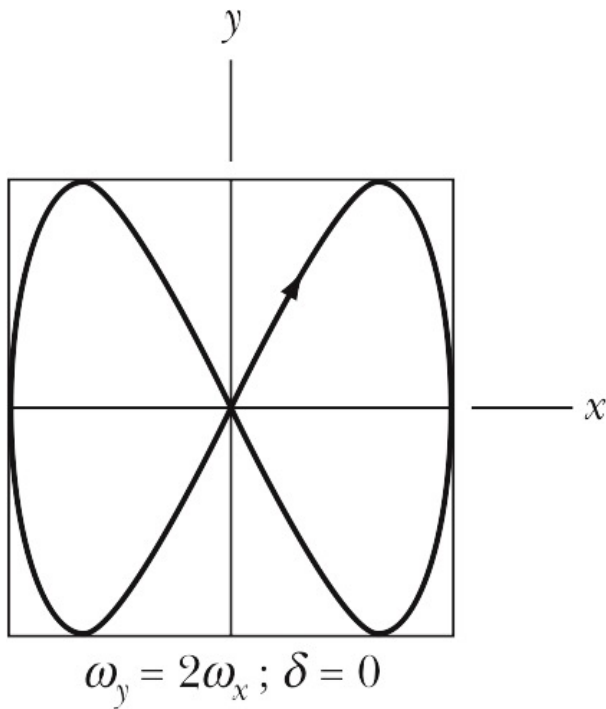


$\delta = 330^\circ$



$\delta = 360^\circ$

# Two-dimensional Simple Harmonic Motion. $y$ vs $x$ for different restoring forces.



# Numerical studies.

---

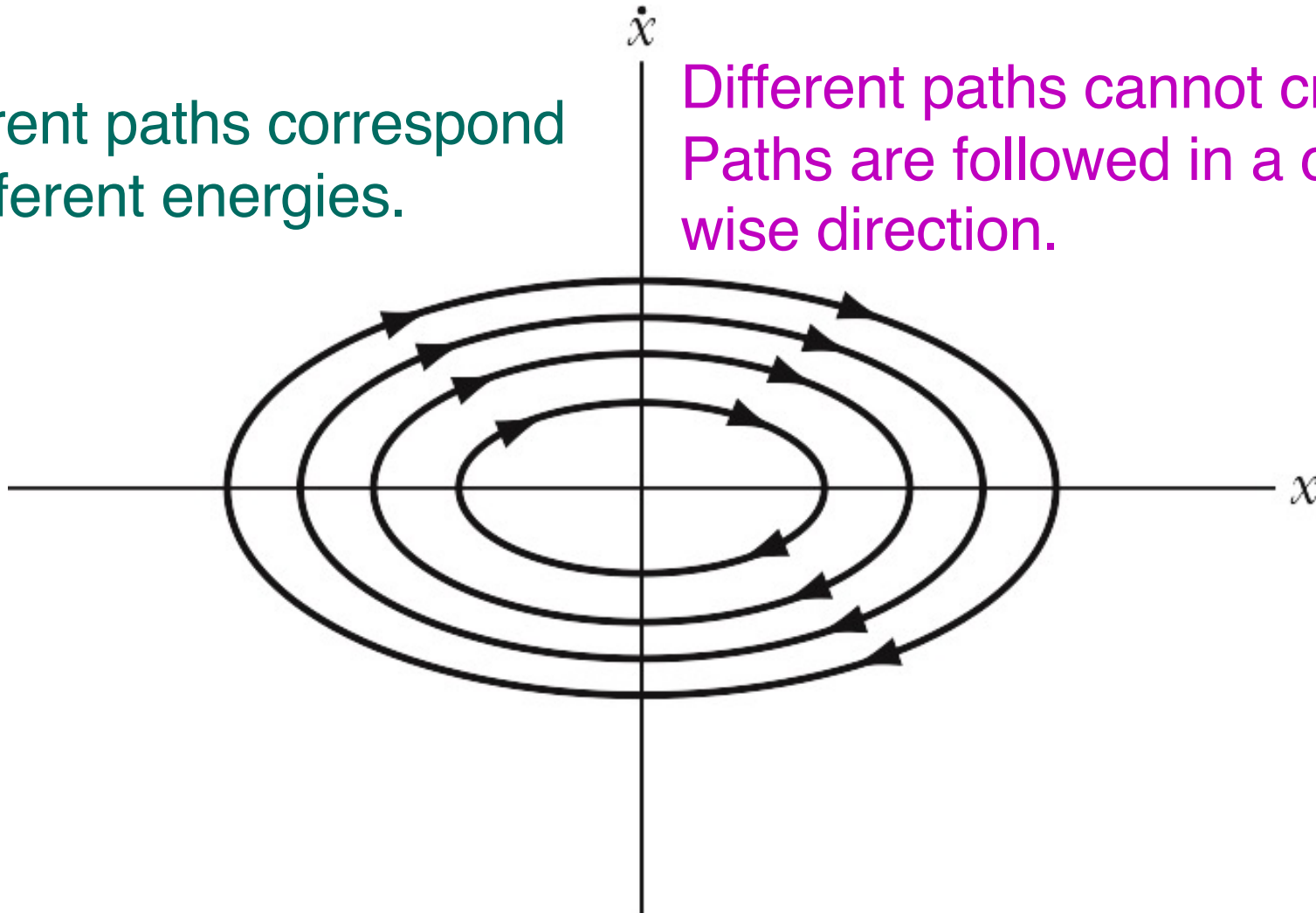
- Using tools such as VPython, it is easy to explore how harmonic motion changes as initial conditions are changed.
- Let us have a look:

<http://www.glowscript.org/#/user/wolfs/folder/Public/program/SimpleHarmonicMotion>

# Phase Diagrams.

Different paths correspond to different energies.

Different paths cannot cross.  
Paths are followed in a clockwise direction.







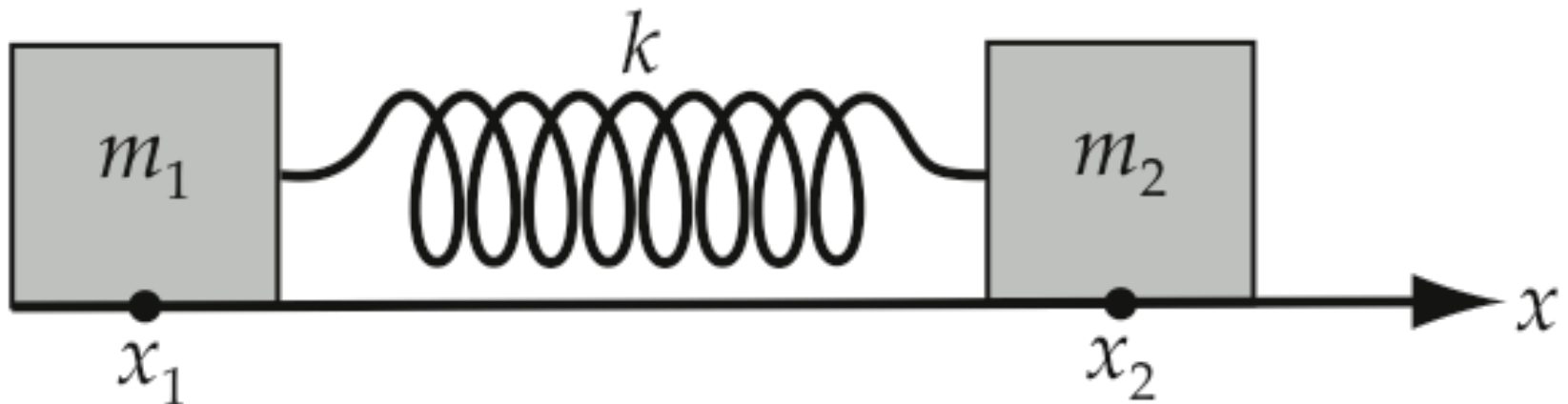
## 2 Minute 18 Second Intermission.

- Since paying attention for 1 hour and 15 minutes is hard when the topic is physics, let's take a 2 minute 18 second intermission.
- You can:
  - Stretch out.
  - Talk to your neighbors.
  - Ask me a quick question.
  - Enjoy the fantastic music.



## Problem 3.6

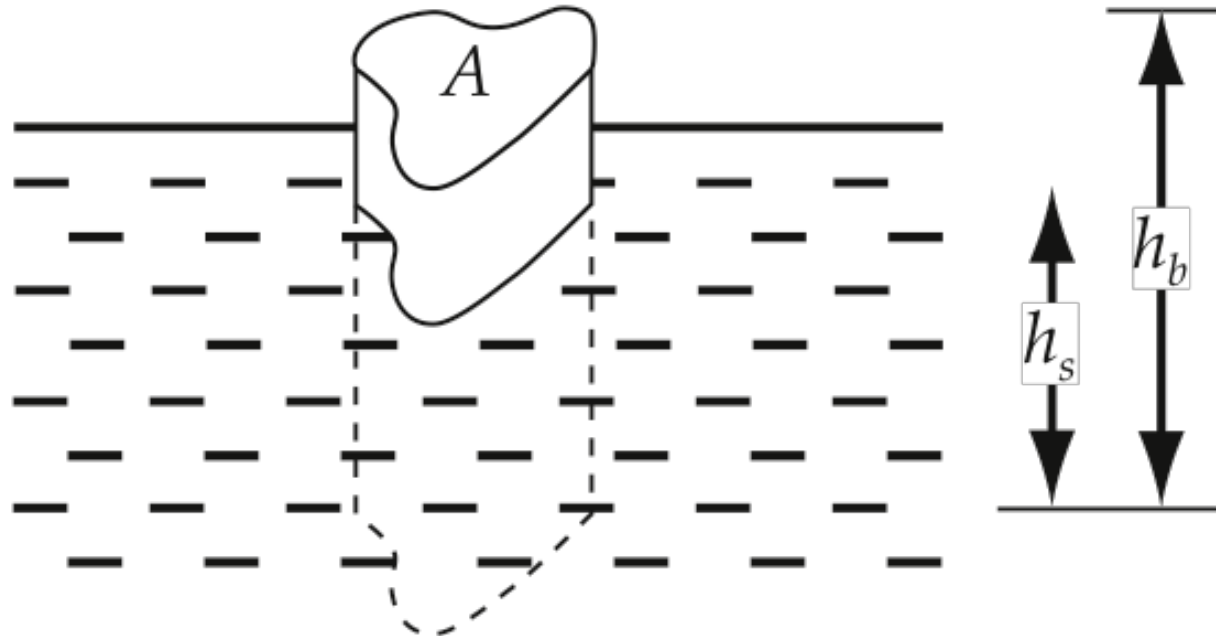
- Two masses  $m_1$  and  $m_2$  slide freely on a horizontal frictionless track and are connected by a spring whose force constant is  $k$ . Find the frequency of oscillatory motion for this system.



## Problem 3.7

- A body of uniform cross-sectional area  $A$  and of mass density  $\rho$  floats in a liquid of density  $\rho_0$ . When it is in equilibrium, the body displaces a volume  $V$ . Show that the period of small oscillations about the equilibrium position is given by

$$\tau = 2\pi \sqrt{\frac{V}{gA}}$$



# Solving Second-Order Differential Equations.

---

- General form:

$$\frac{d^2 y}{dx^2} + a \frac{dy}{dx} + by = f(x)$$

- If you find two linearly independent solutions, every other solution will be a linear combination of these two solutions.
- The general solution has two constants, defined by the initial conditions.
- **Homogeneous equation:**
  - $f(x)$  is equal to 0.
- **Inhomogeneous equation:**
  - $f(x)$  is not equal to 0.

# Homogeneous Equation: $\frac{d^2y}{dx^2} + a\frac{dy}{dx} + by = 0$

---

- Three different scenarios:
  - $a^2 > 4b$
  - $a^2 = 4b$
  - $a^2 < 4b$

# Inhomogeneous Equation: $\frac{d^2y}{dx^2} + a\frac{dy}{dx} + by = f(x)$

---

- Suppose:

- $v$  is a solution of the inhomogeneous equation.
- $u$  is the general solution of the homogeneous equation.

- Then:

- $u + v$  is the general solution of the inhomogeneous equation.

---

# ENOUGH FOR TODAY?