

Physics 141.  
Lecture 23.



The first and the best airline in the world.

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December 5<sup>th</sup>.  
An important day in the Netherlands.



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Physics 141.  
Lecture 23.

- Course information:
  - Laboratory # 5 – lab report is due on Wednesday 12/6 at noon.
  - Homework set # 10 is due on Friday 12/8 at noon.
  - Results Exam # 3.
- Quiz
- Finish the discussion of Chapter 12:
  - The energy distribution of an ideal gas.
  - How do we confirm the energy distribution?
- Start the discussion of Supplement S1, Gases and Heat Engines:
  - The ideal gas law.

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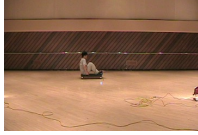
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## Analysis of experiment # 5. Updated Timeline.

- ✓ 11/14: collisions in the May room
- ✓ 11/20: analysis files available.
  - <https://www.pas.rochester.edu/~tdimino/phy141/lab05/>
- ✓ 11/20: each student has determined his/her best estimate of the velocities before and after the collisions (analysis during regular lab periods).
- ✓ 11/21: complete discussion and comparison of results with colliding partners and submit final results (velocities and errors).
- ✓ 11/25: results will be compiled, linear momenta and kinetic energies will be determined, and results will be distributed.
- ✓ 12/4: office hours by lab TA/TIs to help with analysis and conclusions.
- 12/6: students submit lab report # 5.



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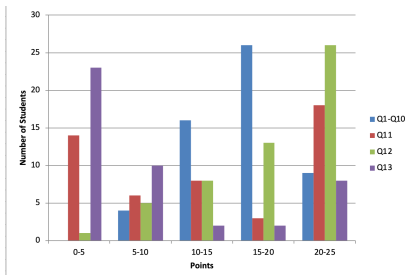
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## Results Exam # 3.



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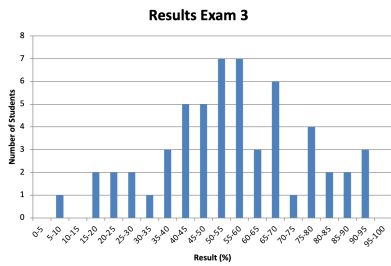
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## Results Exam # 3.



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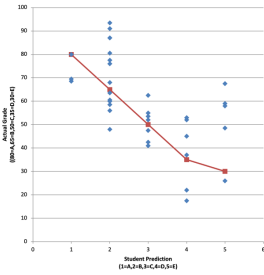
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### Results Exam # 3.



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### Quiz lecture 23.

[PollEv.com/frankwolfs050](https://www.poll Everywhere.com/frankwolfs050)

- The quiz today will have three questions.
- I will collect your answers electronically using the Poll Everywhere system.
- You have 30 seconds to answer each question.



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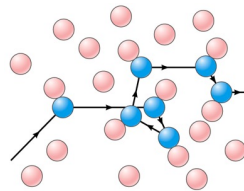
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### Probing molecular speed. The mean-free path.

- The RMS velocities of individual gas molecules are large. For example, for hydrogen at room temperature, the RMS velocity is 1920 m/s.
- Despite the large RMS velocity, the average diffusion velocity is much smaller and is largely determined by the mean-free path of the molecules.
- We expect that the mean-free path is inversely proportional to the cross-sectional area of the molecules and inversely proportional to the density.



Typical values of the mean-free path are between  $10^{-8}$  and  $10^{-7}$  m

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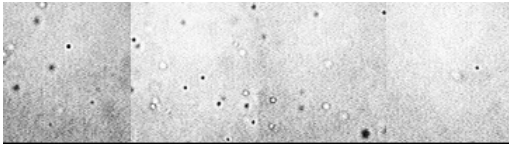
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## Probing molecular speeds in liquids.

0.5  $\mu\text{m}$  particles in water, 50/50 glycerol-water, 75/25 glycerol-water, glycerol



<http://www.physics.emory.edu/~weeks/squishy/BrownianMotionLab.html>

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## Chapter 13. Aka Supplement S1.

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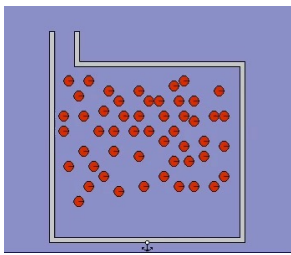
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## Supplement S1. The kinetic theory of gases.



<http://eml.ou.edu/Physics/module/thermal/ketcher/ldg4.avi>

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## The kinetic theory of gases. Thermodynamic variables.

- The kinetic theory of gases provides a framework to connect the microscopic properties of the molecules in a gas (such as their rms velocity) to the macroscopic properties of the gas (such as volume, temperature, and pressure).
- The volume of a gas is defined by the size of the enclosure of the gas. During a change in the state of a gas, the volume may or may not remain constant (this depends on the procedure followed).
- The temperature of a gas has been defined in terms of the entropy of the system (see discussion in Chapter 12).
- We will now briefly discuss pressure.

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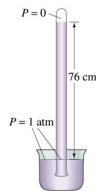
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## Thermodynamic variables. Pressure.

- Pressure is an important thermodynamic variable.
- Pressure is defined as the force per unit area.
- The SI unit is pressure is the Pascal:  $1 \text{ Pa} = 1 \text{ N/m}^2$ . Another common unit is the atm (atmospheric pressure) which is the pressure exerted by the atmosphere on us ( $1 \text{ atm} = 1.013 \times 10^5 \text{ N/m}^2$ ).
- A pressure of 1 atm will push a mercury column up by 76 cm.



Note: if we would use water, the column would be about 10 m high.

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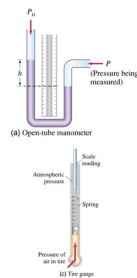
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## Thermodynamic variables. Pressure.

- Many devices that measure pressure, actually measure the pressure difference between the pressure of interest and the atmospheric pressure.
- Atmospheric pressure changes with altitude. The higher you go, the less air is pressing on your head! Airplanes use the atmospheric pressure to measure altitude.
- But keep into consideration that the atmospheric pressure at a fixed location and altitude is not constant!



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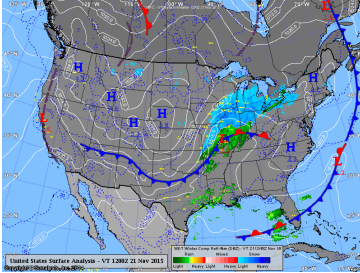
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## Thermodynamic variables. Pressure.



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## The kinetic theory of gases. Thermodynamic variables.

- The **volume** of a gas is defined by the size of the enclosure of the gas. During a change in the state of a gas, the volume may or may not remain constant (this depends on the procedure followed).
- The **temperature** of a gas has been defined in terms of the entropy of the system (see discussion in Chapter 12).
- The **pressure** of a gas is defined as the force per unit area. The SI unit of pressure is the Pascal:  $1 \text{ Pa} = 1 \text{ N/m}^2$ . Another common unit is the atm (atmospheric pressure) which is the pressure exerted by the atmosphere on us ( $1 \text{ atm} = 1.013 \times 10^5 \text{ N/m}^2$ ).

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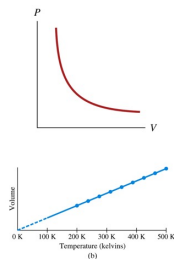
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## The equation of state of a gas.

- In order to specify the state of a gas, we need to measure its temperature, its volume, and its pressure. The relation between these variables and the mass of the gas is called the **equation of state**.
- The equation of state of a gas was initially obtained on the basis of observations.
  - Boyle's Law (1627 - 1691):  
 $pV = \text{constant}$  for gases maintained at constant temperature.
  - Charles's Law (1746 - 1823):  
 $V/T = \text{constant}$  for gases maintained at constant pressure.
  - Gay-Lussac's Law (1778 - 1850):  
 $p/T = \text{constant}$  for gases maintained at constant volume



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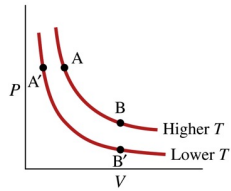
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## The equation of state of a gas.

- Combining the various gas laws we can obtain a single more general relation between pressure, temperature, and volume:  $pV = \text{constant } T$ .



- Another observation that needs to be included is the dependence on the amount of gas: if pressure and temperature are kept constant, the volume is proportional to the mass  $m$ :  $pV = \text{constant } mT$ .

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## The equation of state of a gas.

- The equation of state of a gas can be written as

$$pV = NkT$$

where

- $p$  = pressure (in Pa).
  - $V$  = volume (in  $\text{m}^3$ ).
  - $N$  = number of molecules of gas (1 mole =  $6.02 \times 10^{23}$  molecules or atoms). Note the number of molecules in a mole is also known as Avogadro's number  $N_A$ .
  - $T$  = temperature (in K).
- Note: the equation of state is the equation of state of an ideal gas. Gases at very high pressure and/or close to the freezing point show deviations from the ideal gas law.

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## 3 Minute 34 Second Intermission.



- Since paying attention for 1 hour and 15 minutes is hard when the topic is physics, let's take a 3 minute 34 second intermission.

- You can:
  - Stretch out.
  - Talk to your neighbors.
  - Ask me a quick question.
  - Enjoy the fantastic music.
  - Solve a WeBWork problem.



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## The equation of state of a gas. Example problem.

- A cylinder contains oxygen at 20°C and a pressure of 15 atm at a volume of 12 l. The temperature is raised to 35°C, and the volume is reduced to 8.5 l. What is the final pressure of the gas?
- Since the amount of gas does not change, we can rewrite the ideal gas law in the following way:  $pV/T = \text{constant}$ . Since we know the initial state, we can determine the missing information about the final state:

$$p_i V_i / T_i = p_f V_f / T_f$$

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## The equation of state of a gas. Example problem.

- The final pressure of the gas is equal to

$$p_f = p_i (V_i / V_f) / (T_f / T_i)$$

- Note:
  - This relation will preserve the units of pressure.
  - The units of volume cancel, and we can keep the volume in units of liters. Note: for whatever we unit we choose, zero volume in SI units, correspond to zero volume in all other units.
  - The units of temperature must be in Kelvin. The temperature ratio  $T_i / T_f = (273.15 + 20) / (273.15 + 35) = 0.951$  when  $T$  is expressed in Kelvin. The ratio would be 0.571 when  $T$  is expressed in Celsius.
- When we use the correct units, we find that  $p_f = 22$  atm.

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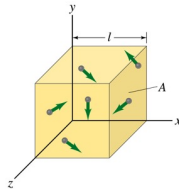
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## The molecular point of view of a gas.

- Consider a gas contained in a container.
- The molecules in the gas will continuously collide with the walls of the vessel.
- Each time a molecule collides with the wall, it will carry out an elastic collision.
- Since the linear momentum of the molecule is changed, the linear momentum of the wall will change too.
- Since force is equal to the change in linear momentum per unit time, the gas will exert a force on the walls.



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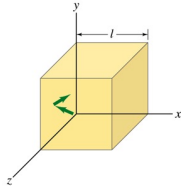
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## The molecular point of view of a gas.

- Consider the collision of a single molecule with the left wall.
- In this collision, the linear momentum of the molecule changes by  $mv_x - (-mv_x) = 2mv_x$ .
- The same molecule will collide with this wall again after a time  $2l/v_x$ .
- The force that this single molecule exerts on the left wall is thus equal to

$$\Delta p/\Delta t = (2mv_x)/(2l/v_x) = mv_x^2/l$$



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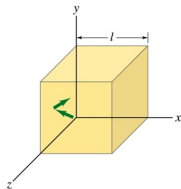
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## The molecular point of view of a gas.

- The force that this single molecule exerts on the left wall is thus equal to
- $$F_{\text{left}} = mv_x^2/l$$
- If the pressure exerted on the left wall by this molecule is equal to
- $$p_{\text{left}} = F_{\text{left}}/A = mv_x^2/(lA)$$
- where  $A$  is the area of the left wall.
- The volume of the gas is equal to  $lA$  and we can thus rewrite the pressure on the left wall:

$$p_{\text{left}} = mv_x^2/V$$



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## The molecular point of view of a gas.

- The pressure that many molecules exerts on the left wall is equal to

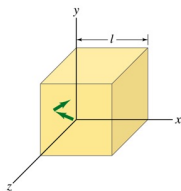
$$p_{\text{left}} = m(v_{1x}^2 + v_{2x}^2 + v_{3x}^2 + \dots)/V$$

- This equation can be rewritten in terms of the average of the square of the x component of the molecular velocity and the number of molecules ( $N$ ):

$$p_{\text{left}} = mN\langle v_x^2 \rangle_{\text{average}}/V$$

- Assuming that there is no preferential direction, the average square of the x, y, and z components of the molecular velocity will be the same:

$$\langle v_x^2 \rangle_{\text{average}} = \langle v_y^2 \rangle_{\text{average}} = \langle v_z^2 \rangle_{\text{average}}$$



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## The molecular point of view of a gas.

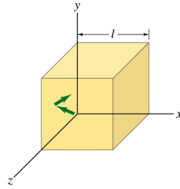
- The force on the left wall can be rewritten in terms of the average squared velocity

$$p_{\text{left}} = mN\langle v^2 \rangle_{\text{average}}/3V$$

- Assuming there is no preferential direction of motion of the molecules, the pressure on all walls will be the same and we thus conclude:

$$pV = mN\langle v^2 \rangle_{\text{average}}/3$$

- Compare this to the ideal gas law:  $pV = NkT$



$$K_{\text{average}} = (1/2)m\langle v^2 \rangle_{\text{average}} = (3/2)kT$$

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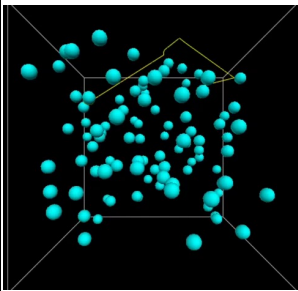
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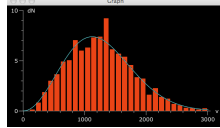
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## Simulating an ideal gas.



- Ideal gas simulations:**
  - Assume elastic collisions between the gas molecules.
  - Assume elastic collisions between the gas molecules and the walls.
- Results agree very well with measured values.



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## Done for today!



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