



Einstein's special theory of relativity

Recall from last time: the special theory of relativity can be reduced to the following two compact statements.

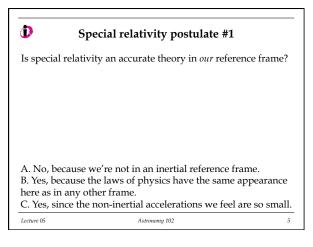
- □ The laws of physics have the same appearance (mathematical form) within all inertial reference frames, independent of their motions.
- □ The speed of light is the same in all directions, independent of the motion of the observer who measures it.

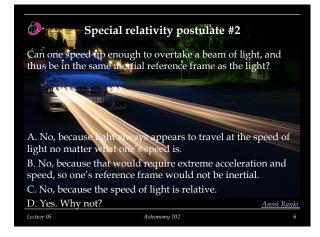
Special = only applies to **inertial reference frames**: those for which the state of motion is not influenced by external forces. Speed of light: measured to be $c = 2.99792458 \times 10^{10}$ cm/sec = 299,792.458 km/sec.

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Einstein's steps in the creation of Special Relativity

Motivation:

- Einstein was aware of the results of the Michelson experiments, and did not accept the explanation of these results by Lorentz in terms of a force, and associated contraction, exerted on objects moving through the aether.
- □ However, he was even more concerned about the complicated mathematical form assumed by the four equations of electricity and magnetism (the Maxwell equations) in moving reference frames, without such a force by the aether. The Maxwell equations are simple and symmetrical in stationary reference frames; he thought they should be simple and symmetrical under all conditions.

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Einstein's steps in the creation of Special Relativity (continued)

Procedure:

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Einstein found that he could start from his two postulates, and show mathematically that in consequence distance and time are relative rather than absolute...
 ...and that distances appear contracted when viewed from moving reference frames, exactly as inferred by Lorentz and Fitzgerald for the "aether force." (This is still called the Lorentz contraction, or Lorentz-Fitzgerald contraction.)
 ...and in fact that the relation between distance and time in differently-moving reference frames is exactly that inferred by Lorentz from the aether-force theory. (This relation is

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still called the Lorentz transformation.)
 He went further to derive a long list of other effects and consequences unsuspected by Lorentz, as follows.

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A list of consequences and predictions of Einstein's special theory of relativity

- (A quick preview before we begin detailed illustrations)
 Spacetime warping: "distance" in a given reference frame is a mixture of distance and time from other reference frames.
- Length contraction: objects seen in moving reference frames appear to be shorter along their direction of motion than the same object seen at rest (Lorentz-Fitzgerald contraction).
- Time dilation: time intervals seen in moving reference frames appear longer than than the same interval seen at rest.
 Velocities are relative, as before (except for that of light),
- but add up in such a way that no speed exceeds that of light.
 There is no frame of reference in which light can appear to be at rest.

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A list of consequences and predictions of Einstein's special theory of relativity (concluded)

- □ Simultaneity is relative: events that occur simultaneously in one reference frame do not appear to occur simultaneously in other, differently-moving, reference frames.
- □ Mass is relative: an object seen in a moving reference frame appears to be *more massive* than the same object seen at rest; masses approach infinity as reference speed approaches that of light. (This is why nothing can go faster than light.)
- □ Mass and energy are equivalent: Energy can play the role of mass, endowing inertia to objects, exerting gravitational forces, *etc.* This is embodied in the famous equation $E = mc^2$.

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Einstein's steps in the creation of Special Relativity (concluded) Impact:

- Einstein's theory achieved the same agreement with experiment as Lorentz, without the need of the unseen aether and the force it exerts, and with other, testable, predictions.
 Einstein's and Lorentz' methods are starkly different.
- Lorentz: evolutionary; small change to existing theories; experimental motivation, but employed "unseen" entities with wait-and-see attitude.
 - Einstein: **revolutionary**; change at the very foundation of physics; "aesthetic" motivation; re-interpretation of previous results by Lorentz and others.
- □ Partly because they were so revolutionary, Einstein's relativity theories were controversial for many years, though they continued to pass all experimental tests.

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